# Hierarchical Models and Chart-Based Decoding 

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12 September, 2013

## Tree-Based Models

- The models we've seen so far operate on sequences of words
- Many translation problems can be best explained by pointing to syntax
- reordering, e.g., verb movement in German-English translation
- long distance agreement (e.g., subject-verb) in output
$\Rightarrow$ Translation models based on tree representation of language
- significant ongoing research
- state-of-the art for some language pairs


## Phrase Structure Grammar

- Phrase structure
- noun phrases: the big man, a house, ...
- prepositional phrases: at 5 o'clock, in Edinburgh, ...
- verb phrases: going out of business, eat chicken, ...
- adjective phrases, ...
- Context-free Grammars (CFG)
non-terminals: phrase structure labels, part-of-speech tags terminals: words
rules: rewrite non-terminal as sequence of Ts and NT
e.g. NP $\rightarrow$ DET NN
- Probabilistic Context-free Grammars (PCFG)
- Attach probabilities to rules


## Parse Tree



Phrase structure grammar tree for an English sentence (as produced Collins' parser)

## Synchronous Context Free Grammar

- English rule

$$
\mathrm{NP} \rightarrow \text { DET JJ NN }
$$

- French rule

$$
\mathrm{NP} \rightarrow \text { DET NN JJ }
$$

- Synchronous rule (indices indicate alignment):

$$
\mathrm{NP} \rightarrow \mathrm{DET}_{1} \mathrm{NN}_{2} \mathrm{JJ}_{3} \mid \mathrm{DET}_{1} \mathrm{JJ}_{3} \mathrm{NN}_{2}
$$

## Synchronous Grammar Rules

- Nonterminal rules

$$
\mathrm{NP} \rightarrow \mathrm{DET}_{1} \mathrm{NN}_{2} \mathrm{JJ}_{3} \mid \mathrm{DET}_{1} \mathrm{JJ}_{3} \mathrm{NN}_{2}
$$

- Terminal rules

$$
\begin{array}{r}
\mathrm{N} \rightarrow \text { maison } \mid \text { house } \\
\mathrm{NP} \rightarrow \text { la maison bleue } \mid \text { the blue house }
\end{array}
$$

- Mixed rules

$$
\mathrm{NP} \rightarrow \text { la maison } \mathrm{JJ}_{1} \mid \text { the } \mathrm{JJ}_{1} \text { house }
$$

## Aligned Tree Pair



Phrase structure grammar trees with word alignment (German-English sentence pair.)

## Reordering Rule

- Subtree alignment

- Synchronous grammar rule
$\mathrm{VP} \rightarrow \mathrm{PPER}_{1} \mathrm{NP}_{2}$ aushändigen $\mid$ passing on $\mathrm{PP}_{1} \mathrm{NP}_{2}$
- Note:
- one word aushändigen mapped to two words passing on ok
- but: fully non-terminal rule not possible


## Rules with Internal Structure

- Subtree alignment

- Synchronous grammar rule (stripping out English internal structure)

$$
\text { PRO/PP } \rightarrow \text { Ihnen } \mid \text { to you }
$$

- Rule with internal structure (Synchronous Tree Substitution Grammar)



## Learning Synchronous Grammars

- Extract rules from a word-aligned parallel corpus
- Hierarchical phrase-based model (hiero)
- only one non-terminal symbol $x$
- no linguistic syntax, just a formally syntactic model
- Synchronous phrase structure model
- non-terminals for words and phrases: NP, VP, PP, ADJ, ...
- corpus must also be parsed with syntactic parser
- restrict extraction to rules compatible with parse
- string-to-tree, tree-to-string, tree-to-tree, ...


## Extracting Phrase Translation Rules



## Extracting Phrase Translation Rules



## Extracting Phrase Translation Rules



- werde Ihnen die entsprechenden Anmerkungen aushändigen
$=$ shall be passing on to you some comments


## Extracting Hierarchical Phrase Translation Rules



## subtracting subphrase

- werde $X$ aushändigen $=$ shall be passing on $X$


## Hierarchical Rule extraction

- All phrase-pairs licensed by PBMT heuristics
- Recursively add hierarchical rules
- So if we have:

$$
\mathrm{X} \rightarrow \text { abc } \mid \text { pqrs } \quad \mathrm{X} \rightarrow \mathrm{~b} \mid \mathrm{qr}
$$

- We can add:

$$
\mathrm{X} \rightarrow \mathrm{aXc} \mid \mathrm{pXs}
$$

- Continue until no more rules can be added
- Rule probabilities derived from frequencies
- Syntax-based models require non-terminals to be constituents


## Hiero Extraction in Practice

- Removal of multiple sub-phrases leads to rules with multiple non-terminals, such as:

$$
\mathrm{Y} \rightarrow \mathrm{X}_{1} \mathrm{X}_{2} \mid \mathrm{X}_{2} \text { of } \mathrm{x}_{1}
$$

- Typical restrictions to limit complexity
- at most 2 nonterminal symbols
- at least 1 but at most 5 words per language
- span at most 15 words (counting gaps)
- Size of europarl-derived fr-en rule table:
- PB: 100M Hiero: 800M


## Overview of Syntactic Decoding



## Overview of Syntactic Decoding



## Syntactic Decoding

Inspired by monolingual syntactic chart parsing:
During decoding of the source sentence, a chart with translations for the $O\left(n^{2}\right)$ spans has to be filled


## Syntax Decoding



German input sentence with tree

## Syntax Decoding



Purely lexical rule: filling a span with a translation (a constituent)

## Syntax Decoding



Purely lexical rule: filling a span with a translation (a constituent)

## Syntax Decoding



Purely lexical rule: filling a span with a translation (a constituent)

## Syntax Decoding



Complex rule: matching underlying constituent spans, and covering words

## Syntax Decoding



Complex rule with reordering

## Syntax Decoding



## Bottom-Up Decoding

- For each span, a stack of (partial) translations is maintained
- Bottom-up: a higher stack is filled, once underlying stacks are complete



## Chart Organization



- Chart consists of cells that cover continuous spans over the input sentence
- Each cell contains a set of hypotheses
- Hypothesis $=$ translation of span with target-side constituent


## Naive Algorithm

Input: Foreign sentence $\mathbf{f}=f_{1}, \ldots f_{l_{f}}$, with syntax tree
Output: English translation e
1: for all spans [start,end] (bottom up) do
2: for all sequences $s$ of hypotheses and words in span [start,end] do
3: for all rules $r$ do
4: $\quad$ if rule $r$ applies to chart sequence $s$ then
5: create new hypothesis $c$
6: add hypothesis $c$ to chart
7: end if
8: end for
9: end for
10: end for
11: return English translation $\mathbf{e}$ from best hypothesis in span $\left[0, l_{f}\right]$

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| :--- | :--- |

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## Solutions

- Recombination
- Stack Pruning
- Prefix tree and Dotted Rules
- Cube pruning


## Dynamic Programming

Rule application creates new hypothesis


## Dynamic Programming

## Another hypothesis



Both hypotheses are indistiguishable in future search $\rightarrow$ can be recombined

## Recombinable States

Recombinable?


## Recombinable States

## Recombinable?



Yes, if max. 2-gram language model is used

## Recombinability

Hypotheses have to match in

- span of input words covered
- output constituent label
- first $n-1$ output words not properly scored, since they lack context
- last $n-1$ output words
still affect scoring of subsequently added words, just like in phrase-based decoding
( $n$ is the order of the $n$-gram language model)


## Stack Pruning

- Number of hypotheses in each chart cell explodes
$\rightarrow$ Only keep a fixed number
- Different stacks for different output constituent labels?
- Cost estimates
- translation model cost known
- language model cost for internal words known
$\rightarrow$ estimates for initial words
- outside cost estimate?
(predict how useful constituent will be later on)


## Storing Rules

- Need to quickly check which rules apply $\rightarrow$ match to available hypotheses and input words
- Example rule

$$
\mathrm{NP} \rightarrow \mathrm{X}_{1} \operatorname{des} \mathrm{X}_{2} \mid \mathrm{NP}_{1} \text { of the } \mathrm{NN}_{2}
$$

- Check for applicability
- Subspan with constituent label NP?
- Input word des?
- Subspan nn?
- Does it apply? - check this sequence:
$\mathrm{NP} \bullet$ des $\bullet \mathrm{NN} \bullet \mathrm{NP}_{1}$ of the $\mathrm{NN}_{2}$
- Use Prefix Tree $\rightarrow$ can check many rules at once


## Prefix Tree for Rules



## Highlighted Rules

$$
\begin{aligned}
& \mathrm{NP} \rightarrow \mathrm{NP}_{1} \mathrm{DET}_{2} \mathrm{NN}_{3} \mid \mathrm{NP}_{1} \mathrm{IN}_{2} \mathrm{NN}_{3} \\
& \mathrm{NP} \rightarrow \mathrm{NP}_{1} \mid \mathrm{NP}_{1} \\
& \mathrm{NP} \rightarrow \mathrm{NP}_{1} \text { des } \mathrm{NN}_{2} \mid \mathrm{NP}_{1} \text { of the } \mathrm{NN}_{2} \\
& \mathrm{NP} \rightarrow \mathrm{NP}_{1} \text { des } \mathrm{NN}_{2} \mid \mathrm{NP}_{2} \mathrm{NP}_{1} \\
& \mathrm{NP} \rightarrow \mathrm{DET}_{1} \mathrm{NN}_{2} \mid \mathrm{DET}_{1} \mathrm{NN}_{2} \\
& \text { NP } \rightarrow \text { das Haus | the house }
\end{aligned}
$$

## Optimising Lookups - Dotted Rules

- If we are trying to match a rule like

$$
\mathrm{p} \rightarrow \mathrm{ABC} \mid \mathrm{x}
$$

... then it helps if we already matched A B to a subspan.

- So store partial matches of the prefix tree
- These are known as Dotted Rules

A B •

## Where are we now?

- Avoid creating hypotheses that cannot be optimal
- Using recombination
- Only keep best scoring hypothesis in each cell
- Stack pruning
- Efficiently organise rules for lookup
- Prefix tree and dotted rules


## Where are we now?

- Avoid creating hypotheses that cannot be optimal
- Using recombination
- Only keep best scoring hypothesis in each cell
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- Efficiently organise rules for lookup
- Prefix tree and dotted rules
- But LM lookup makes hypothesis combination so slow!
$\rightarrow p($ saw $\mid$ the man $) \neq p($ saw $) p($ the $\mid$ man $)$


## Filling a Constituent



## Naive Beam Search

|  | man | -3.6 | the man | $-\mathbf{4 . 3}$ | some men | -6.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| seen -3.8 | seen man -8.8 | seen the man -7.6 | seen some men | -9.5 |  |  |
| saw -4.0 | saw man -8.3 | saw the man | -6.9 | saw some men | -8.5 |  |
| view -4.0 | view man -8.5 | view the man -8.9 | view some men -10.8 |  |  |  |

## Cube Pruning

man -3.6 the man -4.3 some men -6.3<br>seen -3.8 Queue<br>saw -4.0<br>view -4.0

## Queue

Hypothesis
$\rightarrow$ seen man

Sum
$-3.8-3.6=-7.4$

## Cube Pruning

```
    man -3.6 the man -4.3 some men -6.3
seen -3.8 seen man -8.8 Queue
saw -4.0 Queue
view -4.0
```


## Queue



## Cube Pruning

|  | man | -3.6 | the man -4.3 | some men | -6.3 |
| :--- | :--- | ---: | :--- | :--- | :--- |
| seen -3.8 | seen man | -8.8 | Queue |  |  |
| saw -4.0 | saw man | -8.3 | Queue |  |  |
| view -4.0 | Queue |  |  |  |  |

## Queue

| Hypothesis | Sum |
| :---: | ---: |
| $\rightarrow$ view man | $-4.0-3.6=-7.6$ |
| seen the man | $-3.8-4.3=-8.1$ |
| saw the man | $-4.0-4.3=-8.3$ |

## Cube Pruning

|  | man | -3.6 | the man -4.3 | some men | -6.3 |
| :--- | :--- | ---: | :--- | :--- | :--- |
| seen -3.8 | seen man | -8.8 | Queue |  |  |
| saw -4.0 | saw man | -8.3 | Queue |  |  |
| view -4.0 | view man -8.5 | Queue |  |  |  |

## Queue



## Cube Pruning

|  | man | -3.6 | the man | -4.3 | some men |
| :--- | :--- | :--- | :--- | :--- | :--- |
| -6.3 |  |  |  |  |  |

## Queue

| Hypothesis | Sum |
| :---: | ---: |
| $\rightarrow$ saw the man | $-4.0-4.3=-8.3$ |
| view the man | $-4.0-4.3=-8.3$ |
| seen some men | $-3.8-6.3=-10.1$ |

## Cube Pruning versus Beam Search

Same Bottom-up with fixed-size beams
Different Beam filling algorithm

## Cube Pruning: Speed vs. Accuracy



## Many Cubes

- Could be several source-side matches for given span
- Create a cube for each one
- One queue per cube - or single queue
$\rightarrow$ Always pop most promising hypothesis


## One Stage or Two Stage Decoding

- First stage: decoding without a language model (-LM decoding)
- Can be done exhaustively
- Eliminate dead ends
- Optionably prune out low scoring hypotheses
- Second stage: add language model
- Limited to packed chart obtained in first stage
- Can do a single pass (interleaved)


Vs.

cdec does 2 passes
but Moses does 1!

## Summary

- Synchronous context free grammars
- Rule extraction from aligned corpus
- Bottom-up decoding
- Chart organization: dynamic programming, stacks, pruning
- Prefix tree for rules
- Dotted rules
- Cube pruning

